

UNITS: λ_D and ω_p

$$\text{Debye length } \lambda_D = \left(\frac{k_B T_e \epsilon_0}{q^2 n_e} \right)^{1/2}; \text{ Plasma } \omega_p = \left(\frac{q^2 n_e}{m_e \epsilon_0} \right)^{1/2}$$

Frequency

where k_B = Boltzmann's constant $1.36 \times 10^{-23} \frac{\text{J}}{\text{K}}$

T_e = Electron temperature (eV)

ϵ_0 = Permittivity of free space = $8.854 \times 10^{-14} \text{ F-cm}^{-1}$

q = elementary charge 1.6×10^{-19} Coulombs

n_e = electron density (cm^{-3})

Note: F (Farad) = $\frac{\text{C}^2}{\text{Joule}}$

$$\lambda_D = \left[\frac{1.36 \times 10^{-23} \frac{\text{J}}{\text{K}} \times T_e \text{ eV} \times 11594.2 \frac{\text{eV}}{\text{K}} \times 8.85 \times 10^{-14} \frac{\text{C}^2}{\text{J-cm}}}{(1.6 \times 10^{-19})^2 \text{ C}^2 \times n_e \left(\frac{1}{\text{cm}^3} \right)} \right]^{1/2}$$

$$= \left[\frac{5.45 \times 10^5 T_e \text{ cm}^2}{n_e} \right]^{1/2} = 738.3 \left[\frac{T_e \text{ (eV)}}{n_e \left(\frac{1}{\text{cm}^3} \right)} \right]^{1/2} \text{ cm}$$

$$\omega_p = \left[\frac{(1.6 \times 10^{-19})^2 \text{ C}^2 \times n_e \left(\frac{1}{\text{cm}^3} \right) \text{ J-cm} \times 10^7 \text{ erg} \times \text{cm}^2 \text{ -g}}{0.911 \times 10^{-27} \text{ g} \times 8.85 \times 10^{-14} \frac{\text{C}^2}{\text{J}} \times \frac{\text{erg}}{\text{s}^2 \text{ -g}}} \right]^{1/2}$$

$$= \left[\frac{3.175 \times 10^9 n_e \left(\frac{1}{\text{cm}^3} \right)}{\text{s}^2} \right]^{1/2}$$

$$= 5.635 \times 10^4 \left[n_e \left(\frac{1}{\text{cm}^3} \right) \right]^{1/2} \frac{\text{Radians}}{\text{s}}$$